

MODIFIED CYCLIC MODEL OF INTERFACES WITH ROUGHENED SURFACE AND DOWEL BAR SUBJECTED TO NORMAL AND SHEAR STRESSES

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Abstract: When reinforced concrete (RC) buildings are seismically retrofitted, new members are attached to existing members through interfaces with roughened surfaces using vibratory hammer and post-installed dowel bars. To attach extended members to the outside of an existing frame, the interfaces are subjected to bending moments and shear forces. In other words, interfaces are subjected to the compressive or tensile normal stresses in addition to shear stresses. However, the previous literature is limited in its investigation of the behaviors under such combined stresses. Therefore, in the authors' previous study, the shear strength estimation of the interfaces was proposed; and then, the cyclic model was presented. Although the proposed model can be applied to the interfaces subjected to tensile and shear stresses, the behavior under compressive normal stress was not discussed. Hence, in this study, the model was improved to estimate the cyclic behavior under the different normal stresses. The Saenz model, which is a constitutive law of concrete, was used to evaluate the envelope behavior. In addition, the peak stress was calculated by using the proposed estimation. For the compressive normal stress, the envelope model and peak stress were modified. Subsequently, the proposed cyclic rules were applied; and, a previous dowel model was incorporated into the modified model. The concrete compressive strength was set to 20-23 N/mm², the diameters of the anchor bar were 13, 16, and 19 mm, the compressive normal stress was set to -0.48 N/mm², and the tensile ratio r_N was set to 0.00, 0.33, and 0.66. Epoxy adhesive was used. As a result, the modified model agreed well with the test results; the average ratio of the test results to the model results was 0.91-1.12. In addition, with the increase of δ , the effect of the dowel bar was intensified; whereas, under the compressive normal stress, it became insignificant. Finally, it was concluded that the modified model could reasonably estimate the behavior under the various stresses.

1 INTRODUCTION

In recent years, the importance of sustainable development goals (SDGs) and decarbonization have been increasing.

Therefore, seismic retrofit is important to use seismically weak concrete structures. When new members are connected to existing members, the concrete surface is roughened and post-installed dowel bars are applied to the

surface. For reinforced concrete (RC) buildings, the roughened surfaces are produced using a vibratory hammer. Fig. 1 illustrates the interfaces between new and existing members. During an earthquake, the interfaces are subjected to shear and normal forces.

In the previous studies, the concrete interfaces and the dowel action are traditional topics. The shear-friction theory was proposed by Mattock [3] in the 1960s. Since the 1980s, the aggregate interlocking has been studied by Walraven et al. [4-5] and Bujadaham [6-7]. Furthermore, many researchers have studied dowel action. Dowel action was started by Friberg [8]. Vintzēleou and Tassios proposed the famous dowel formula. [9] Sorensen introduced catenary actions to dowels. [10]

Moreover, the authors studied a roughened surface by a hammer and post-installed dowel bars. [1-2,11-16]. In the studies, the interfaces and the post-installed dowel bars were subjected to the tensile and shear stresses. However, the mechanical model was not proposed. Therefore, in this study, the previous model was modified to apply to the mechanical behavior under the shear and compressive normal stresses.

Section 2 describes the outline of the test, Section 3 explains the modified model, Section 4 discusses the model accuracy, and finally, Section 5 describes the conclusions.

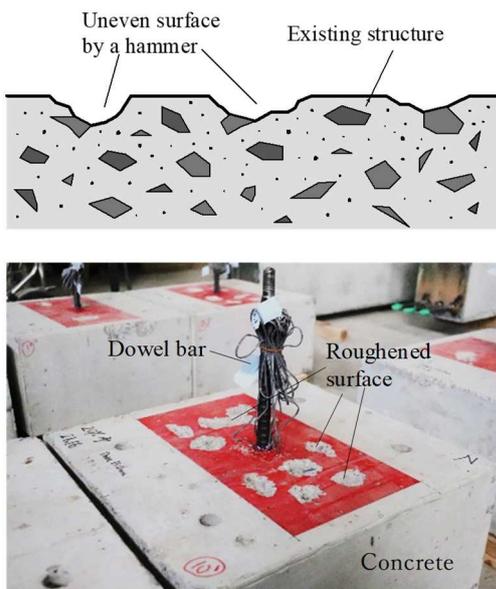


Fig. 1: Examples of interfaces. [1-2]

2 OUTLINE OF LOADING TEST

The previous test results [1] were used to verify the accuracy of the modified model. Therefore, the outline of the shear loading tests is briefly explained in this section.

2.1 Test parameters

The test parameters are listed in Table 1.

The test parameters were the diameter of the anchor bolt d_d , the roughness ratio r_{rc} , and the normal stress. The d_d and r_{rc} were set to 13, 16, 19 mm and 0.1, 0.2, 0.3, respectively.

The r_{rc} is obtained by the following equation.

$$r_{rc} = \frac{A_{hrc}}{A_j} \quad (1)$$

where A_j and A_{hrc} are the interface area and the horizontal projection area of the uneven surface, respectively.

Table 1: Test parameters.

Specimen ID	σ_0 or r_N	r_{rc}	Anchor bar			Conc. & grout		
			Tar.	Mea.	d_d	f_y	E_s	f_c
D13R01C ₀₄₈	-0.48	0.1	0.115	13	403	174	22.5	68.0
D13R02C ₀₄₈	-0.48	0.2	0.206	13	403	174	20.1	69.2
D13R03C ₀₄₈	-0.48	0.3	0.316	13	403	174	22.5	68.0
D16R01C ₀₄₈	-0.48	0.1	0.107	16	387	175	20.1	69.2
D16R02C ₀₄₈	-0.48	0.2	0.190	16	387	175	20.1	69.2
D16R03C ₀₄₈	-0.48	0.3	0.302	16	387	175	20.1	69.2
D13R01T ₀₀₀	0.00	0.1	0.098	13	381	171	23.0	65.6
D13R01T ₀₃₃	0.33	0.1	0.106	13	381	171	23.0	65.6
D13R01T ₀₆₆	0.66	0.1	0.107	13	381	171	23.0	65.6
D13R02T ₀₀₀	0.00	0.2	0.194	13	381	171	23.0	65.6
D13R02T ₀₃₃	0.33	0.2	0.210	13	381	171	23.0	65.6
D13R02T ₀₆₆	0.66	0.2	0.199	13	381	171	23.0	65.6
D13R03T ₀₀₀	0.00	0.3	0.300	13	381	171	23.0	65.6
D13R03T ₀₃₃	0.33	0.3	0.318	13	381	171	23.0	65.6
D13R03T ₀₆₆	0.66	0.3	0.304	13	381	171	23.0	65.6
D16R01T ₀₀₀	0.00	0.1	0.093	16	387	175	20.8	62.9
D16R01T ₀₃₃	0.33	0.1	0.094	16	387	175	20.8	62.9
D16R01T ₀₆₆	0.66	0.1	0.106	16	387	175	20.8	62.9
D16R02T ₀₀₀	0.00	0.2	0.196	16	387	175	20.8	62.9
D16R02T ₀₃₃	0.33	0.2	0.199	16	387	175	20.8	62.9
D16R02T ₀₆₆	0.66	0.2	0.210	16	387	175	20.8	62.9
D16R03T ₀₀₀	0.00	0.3	0.301	16	387	175	20.8	62.9
D16R03T ₀₃₃	0.33	0.3	0.294	16	387	175	20.8	62.9
D16R03T ₀₆₆	0.66	0.3	0.292	16	387	175	20.8	62.9
D19R01T ₀₀₀	0.00	0.1	0.095	19	391	176	23.0	65.6
D19R01T ₀₃₃	0.33	0.1	0.102	19	391	176	23.0	65.6
D19R01T ₀₆₆	0.66	0.1	0.096	19	391	176	23.0	65.6
D19R02T ₀₀₀	0.00	0.2	0.215	19	391	176	23.0	65.6
D19R02T ₀₃₃	0.33	0.2	0.203	19	391	176	23.0	65.6
D19R02T ₀₆₆	0.66	0.2	0.204	19	391	176	23.0	65.6
D19R03T ₀₀₀	0.00	0.3	0.307	19	391	176	23.0	65.6
D19R03T ₀₃₃	0.33	0.3	0.304	19	391	176	23.0	65.6
D19R03T ₀₆₆	0.66	0.3	0.304	19	391	176	23.0	65.6

d_d [mm]: the diameter of anchor bar. f_y [N/mm²] and E_s [kN/mm²]: the yield strength and Young's modulus of dowel bar, respectively.

The compressive normal stress was set to -0.48 N/mm^2 . For the tensile normal stress, the tensile ratio r_N , which is the ratio of the stress to the yield strength of anchor bolt, was used; and, set to 0.00, 0.33, and 0.66.

The material properties of the dowel bar, concrete, and grout are also listed in **Table 1**. The concrete used for the specimens was $f_c = 20 \text{ N/mm}^2$; and, the material tests were based on JIS standards [17,18]. Here, the hole diameter $d_h = 16, 22, \text{ and } 25 \text{ mm}$ for $d_d = 13, 16, \text{ and } 19 \text{ mm}$, respectively. Young's modulus of concrete $E_c = 17.4, 21.8, 17.5 \text{ and } 16.4 \text{ kN/mm}^2$ for $f_c = 22.5, 20.1, 23.0 \text{ and } 20.8 \text{ N/mm}^2$, respectively. Young's modulus of grout $E_g = 25.9, 27.2, 26.4 \text{ and } 24.4 \text{ kN/mm}^2$ for $f_g = 68.0, 69.2, 65.6 \text{ and } 62.9 \text{ N/mm}^2$, respectively.

2.2 Test specimen

The outline of the shear loading test is shown in **Fig. 2** (a). The specimens consisted of concrete and mortar blocks with dimensions of $440 \text{ mm} \times 460 \text{ mm} \times 250 \text{ mm}$ and $375 \text{ mm} \times 200 \text{ mm} \times 190 \text{ mm}$, respectively. Plywood was used for the formwork of specimen. In addition, the concrete was cast vertically; therefore, the interface was smooth and greased. The effect of friction was low. After curing for 28 days, the surfaces were roughened by using a hammer. The anchor bolts were then adhered by using a diamond core drill and epoxy adhesive.

2.1 Shear loading test

The loading setup was used shown in **Fig. 2** (b). One 500-kN hydraulic jack was used for shear loading. In addition, two 150-kN screw jacks were used for normal stress loading. Four displacement sensors were used to measure the slip δ and opening ω . The measured ω was required for a PID (proportional–integral–derivative) auto-control system. With PID auto-control, the surface moved horizontally during shear loading and the normal stress was maintained at the target value. A static shear load was applied to the specimens. The load cycle was $\pm 0.125, \pm 0.25, \pm 0.50, \pm 1.0, \pm 1.5, \pm 2.0, \pm 3.0, \pm 4.0, \pm 6.0, \text{ and } \pm 8.0 \text{ mm}$.

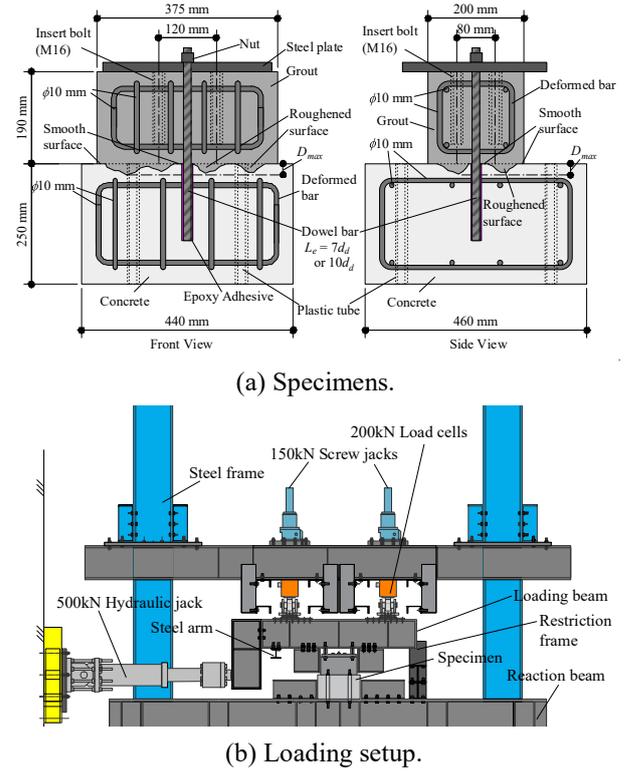


Fig. 2: Outline of shear loading test.

3 MODIFIED MODEL

The authors proposed the cyclic model of the interface with a dowel bar and a roughened surface. In this section, the modification of the model is explained. In addition, the outlines of the original model are briefly explained.

3.1 Dowel model

The dowel model, which has been proposed in previous studies, was used in the modified model. **Fig. 3** shows a picture of the dowel model. In **Fig. 3**, the σ_b is the bearing stress of concrete, M_s is the full plastic bending moment at the plastic hinge, and σ_t is the tensile stress of the anchor bolt by a catenary action. [11-14]

The shear force Q_d is expressed as follows:

$$Q_d = q_s + q_B + q_T^S \quad (2)$$

where q_s is the shear force caused by the bending moment of the plastic hinge, q_B is the bearing stress, and q_T^S is the shear force by the catenary action. These stresses can be calculated by using M_s , σ_b , and σ_t , respectively.

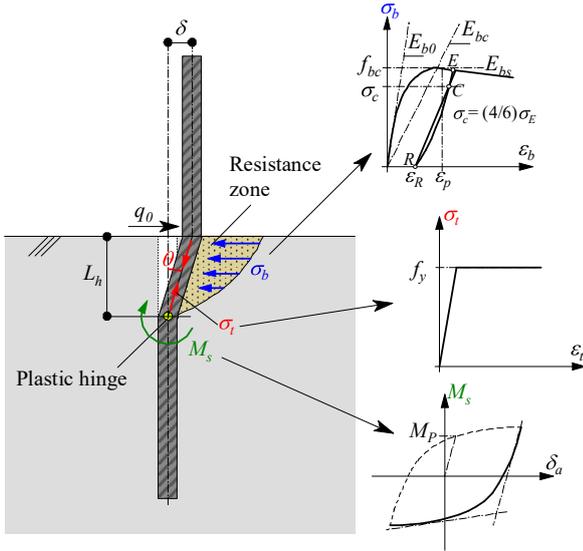


Fig. 3: Image of the dowel model. [11-14]

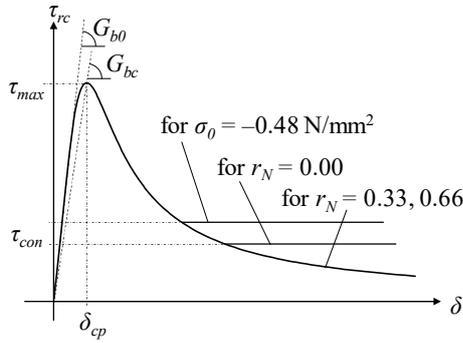


Fig. 4: Envelope curve for roughened surface. [2]

3.2 Modified roughened surface model

In the previous study [2], the authors constructed the original model for the roughened surface. The original model can be applied to the specimens subjected to the tensile and shear stresses. In this study, the model was improved to estimate the behavior under the compressive normal stress.

3.2.1 Envelope curve

The following equation was used to model the envelope curve. [2]

$$\tau_{rc} = \frac{G_{b0} \cdot \delta}{1 + \left(\frac{G_{b0}}{G_{bc}} - 2\right) \left(\frac{\delta}{\delta_{cp}}\right) + \left(\frac{\delta}{\delta_{cp}}\right)^\beta} \quad (3)$$

where G_{b0} and G_{bc} are the initial stiffness and

angle of the line passing through the original and peak points, respectively. This equation was constructed using the Saenz model [19]. G_{b0} and δ_{cp} are set to $6.9 \text{ N/mm}^2/\text{mm}$ and $= 0.50 \text{ mm}$, respectively. [2] In the Saenz model [18], $\beta = 2$ was employed. In this study, to express the stress-softening behavior of the roughened surface, the modified β was used as follows.

$$\beta = 3.5 \cdot r_N + 2.5 \geq 2.0 \quad (4)$$

Here, for the specimen subjected to the compressive normal stress, σ_0 is used instead of r_N .

Moreover, for the specimen with $\sigma_0 = -0.48 \text{ N/mm}^2$ and $r_N = 0.00$, Q converged to a constant value. Therefore, τ_{con} , that is the constant shear stress after softening, is used; and, expressed by the following equation:

$$\tau_{con} = \begin{cases} -\sigma_0 & \text{for the comp. stress} \\ 0.3 & \text{for } r_N = 0.00 \\ 0.0 & \text{for } r_N > 0.00 \end{cases} \quad (5)$$

These values are obtained from the average stress with $\delta = 2-6 \text{ mm}$.

Furthermore, the shear strength formula was proposed. [2] In the equation, the uneven surface was considered as a cone; and, with based on the previous study, the shear strength τ_{max} was expressed by vertical projection area of the uneven surface and the value of the exponent of f_c . Then, the value of $\tau_{max,p}$, that is the maximum shear stress on the positive side, is calculated by the following equation:

$$\tau_{max,p} = \left(\frac{r_{rc} D_{max}}{3\sqrt{\pi}} f_c^{0.24} + 0.13 \right) \times (1 - N) \quad (6)$$

where D_{max} is 12.6 mm , which is the average value of the specimens. N is the value of r_N or σ_0 . To consider the effect by the normal stress, the function of $(1-N)$ is employed.

The minimum shear force on the negative side is calculated as follows:

$$\tau_{max,n} = 0.9 \times \tau_{max,p} \quad (7)$$

3.2.2 Unloading behavior

The cyclic model is illustrated in Fig. 5. Points B and C are the start and end points of the unloading curve, respectively. Point Z

represents the intersection of the unloading and reloading curves. The parabolic function was used for the unloading behavior. This model passes through Points B and C in Fig. 5. δ_B and δ_C are the shear displacements of Points B and C, respectively; and, are expressed as follows.

$$\delta_C = 0.9 \cdot \delta_B \quad (8)$$

Here, Point C is the vertex of the parabolic function, therefore, the following equations are obtained for the unloading behavior.

$$\tau_{rc} = \gamma(\delta - \delta_C)^2 \quad (9)$$

$$\gamma = \frac{\tau_B}{(0.1 \cdot \delta_B)^2} \quad (10)$$

3.2.3 Reloading behavior

As well, the reloading behavior starts from the original Point O; and, the behavior is the linear function. Point Z, that is the intersection of the unloading and reloading behaviors, is expressed as follows:

$$\tau_Z = \begin{cases} 0.5\tau_B & \text{for } r_N = 0.00 \sim 0.66 \\ \frac{2}{3}\tau_B & \text{for } \sigma_0 = -0.48 \text{ N/mm}^2 \end{cases} \quad (11)$$

where, τ_Z is the shear stress of Point Z. In this study, the lower equation of Eq. (11) was added for the compressive normal stress. The reloading behavior τ_{rc} can be obtained as follows:

$$\tau_{rc} = \frac{\tau_Z}{\delta_Z} \cdot \delta \quad (12)$$

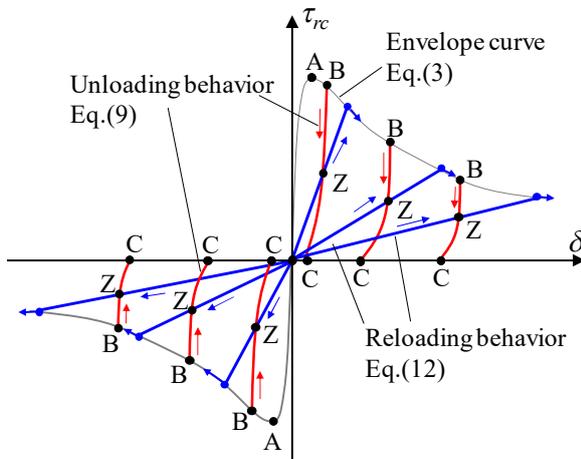


Fig. 5: Cyclic rules for the roughened surface.

After the reloading line crosses the envelope curve, τ_{rc} is expressed by Eq. (3).

3.2.4 Coefficient for effect of d_d

As mentioned in the previous paper [2], when d_d was smaller, the opening was wider; therefore, for the specimen with $d_d = 13$ mm, the previous model overestimated the test results. Fig. 6 shows the relationship between α and d_d . Here, α is the safety factor, which can be obtained by dividing Q_{max} by Q_{cat} . According to Fig. 6, the medians for $d_d = 16$ and 19 mm are almost the same. Whereas the median for $d_d = 13$ mm is smaller than that for $d_d = 16$ and 19 mm.

Hence, in this study, K_α , that is the coefficient to evaluate the effect of d_d , was used and is described as the follows:

$$K_\alpha = \begin{cases} 0.05d_d + 0.2 & \text{for } 13 \leq d_d < 16 \\ 1.0 & \text{for } d_d \geq 16 \end{cases} \quad (13)$$

From the above, the analytical shear load Q_{Ana} is expressed by the following equation.

$$Q_{Ana} = Q_{d,ave} + Q_{rc} \quad (14)$$

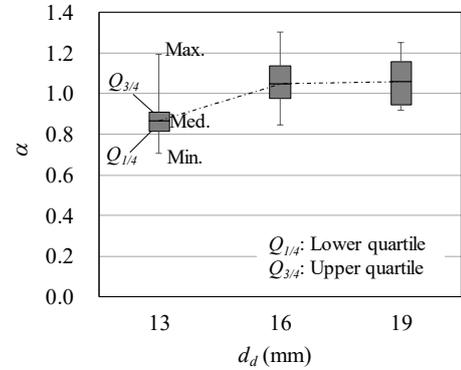


Fig. 6: Relation between α and d_d .

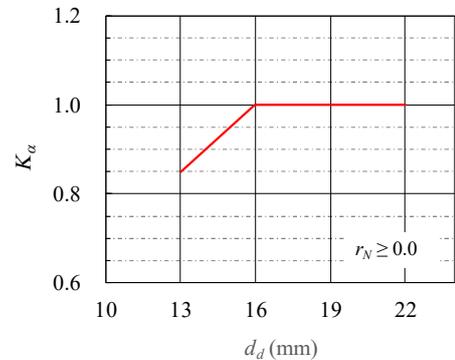


Fig. 7: Relation between K_α and d_d .

$$Q_{rc} = K_{\alpha} \times A_j \times \tau_{rc} \quad (15)$$

where $Q_{d,ave}$ is obtained by Eq. (2), with $\delta = 0.46$ mm, which is the average shear displacement during Q_{max} .

4 DISCUSSION

This section compares the analytical values of the proposed model with the test results. In addition, the failure mode was briefly explained.

4.1 Test results

Fig. 8 shows the failure mode of the specimens. As shown in **Fig. 8**, the bearing damage was confirmed around the dowel bars and uneven surfaces. Similar damage was also observed in the other specimens. Therefore, the specimens were failed by dowel action and bearing stress on the roughened surface.

4.2 $Q-\delta$ curves

Figs. 9–11 show the $Q-\delta$ curves for $d_d = 13$, 16, and 19 mm, respectively. The blue lines are the calculated results of the dowel model.

4.2.1 $d_d = 13$ mm

From **Fig. 9** (i)-(iv) with $r_{rc} = 0.1$, the proposed models reasonably estimate the four test results. For $r_N = 0.33$ and 0.66, the dowel models are corresponding with the test results after $\delta = 2$ mm.

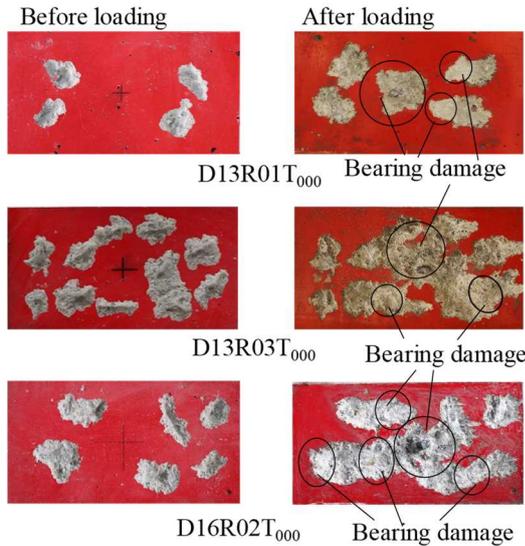


Fig. 8: Failure modes.

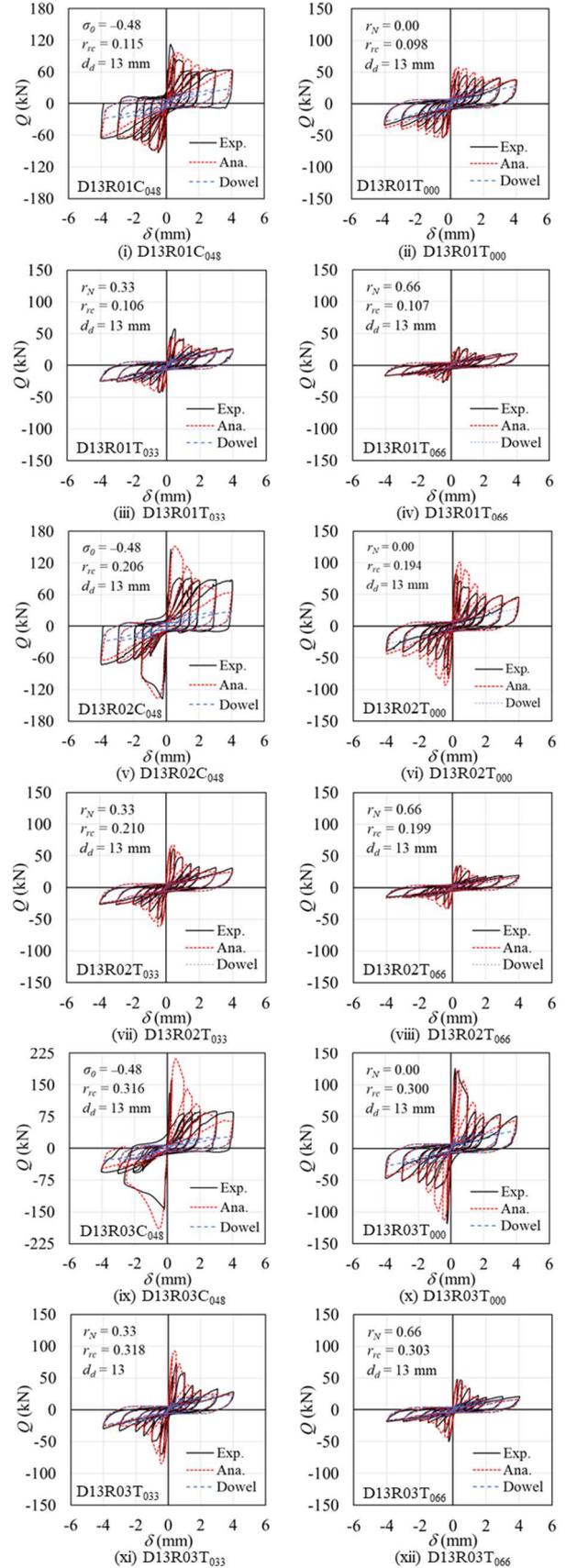


Fig. 9: $Q-\delta$ curves for $d_d = 13$ mm.

Therefore, when the interfaces are subjected to the tensile stress, only the dowel bars resist to the shear force in the large displacement region.

Focusing on the results of D13R02C₀₄₈ and D13R03C₀₄₈ in **Fig. 9** (v) and (ix), the proposed model cannot estimate the test result from $\delta = +0.25$ mm to +1 mm. In these specimens, the large slip behavior was observed on the negative side. Therefore, after $\delta = +0.25$ mm, the shear force was smaller than the other specimens. Hence, the model could not estimate the irregular behavior. In addition, the large slip behavior was observed for the specimens with $\sigma_0 = -0.48$ N/mm². Expect for these two specimens, the proposed model can reasonably estimate the envelope curve, unloading behavior, and the reloading behavior of the test results.

4.4.2 $d_d = 16$ mm

Fig. 10, that shows the results of the specimen with $d_d = 16$ mm, is observed. Focusing on the specimens with $\sigma_0 = -0.48$ N/mm², the large slips that were confirmed in **Fig. 9** are not observed. Thus, as the d_d becomes smaller, the dowel effect decreases; therefore, the specimens failed brittle. However, the model overestimates the peak forces for the specimens with $\sigma_0 = -0.48$ N/mm² in **Fig. 10** (v) and (ix). As shown in **Fig. 9**, for some of the tests, the model could not estimate well. However, for most of the specimens, the analytical results by the model are in good agreement with the test results.

4.2.3 $d_d = 19$ mm

Finally, **Fig. 11** is focused. The specimens with $d_d = 19$ mm were only subjected to the tensile normal and shear stresses; thus, the compressive normal stress was not applied.

As well as the specimens with $r_N = 0.00-0.66$ in **Figs. 9** and **10**, the proposed model reasonably estimates the test results.

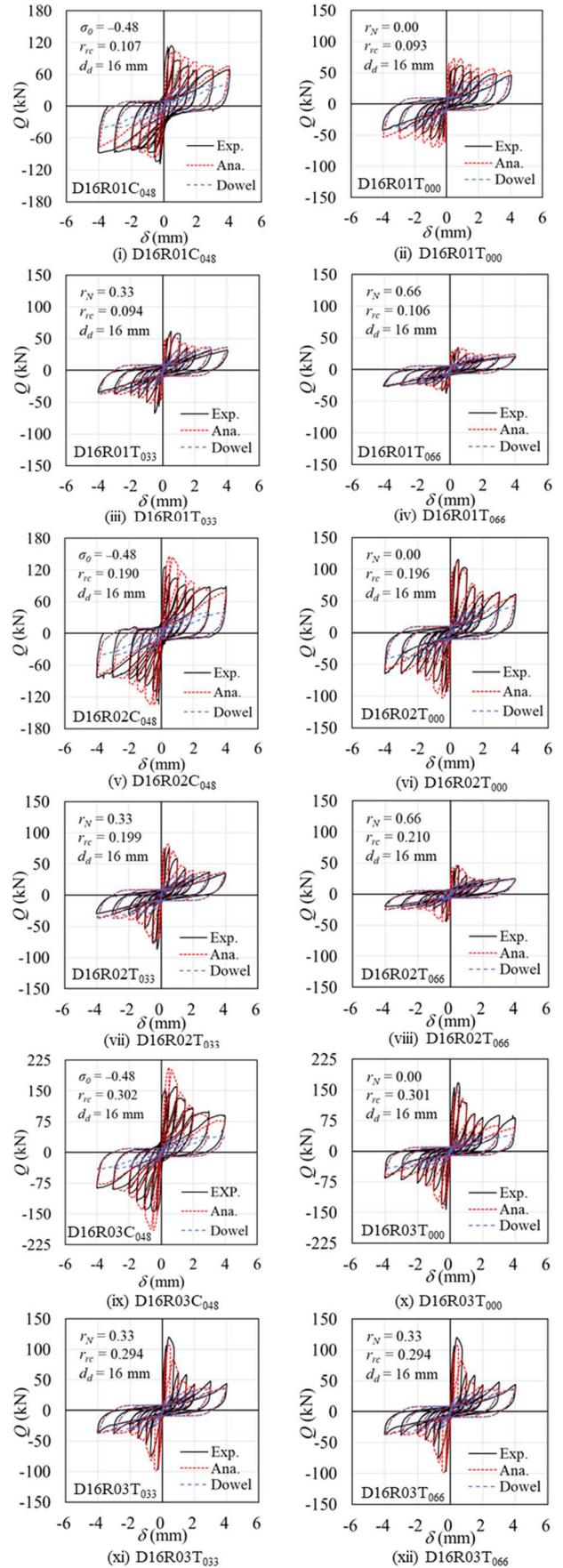


Fig. 10: Q - δ curves for $d_d = 16$ mm.

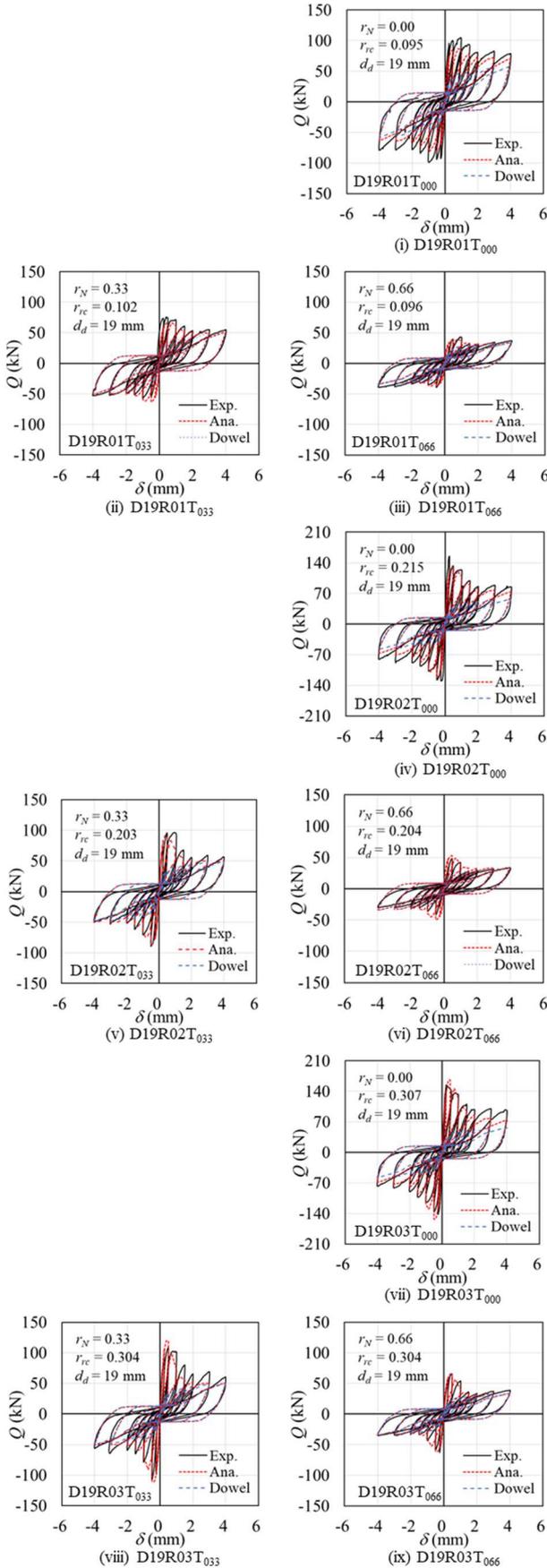


Fig. 11: Q - δ curves for $d_d = 19$ mm.

As mentioned earlier, except for the irregular behavior, the modified model is useful for estimating the mechanical behavior of the interface with the post-installed anchor and the roughened surface subjected to the normal and shear stresses.

4.2.4 Dowel action

In the section, the blue lines of **Figs. 9-11**, which indicate the result of dowel action, are focused. In all figures, when δ is smaller, the gaps between the test results and the dowel model are larger. Therefore, the effect of the roughened surface on the shear resistance is greater. As δ increased, the effect of the dowel bar became significant. Moreover, when the surface was subjected to the compressive normal stress, the effect of the dowel bar became less significant than that of the tensile normal stress.

4.3 Model to test shear force ratio

Table 2 lists the test to model shear force ratio R_{t2m} . As mentioned in Section 4.2, the irregularities were confirmed for the specimens with $d_d = 13$ mm and $\sigma_0 = -0.48$ N/mm²; and, in these case, the analytical results did not agree well with the test results. Thus, the R_{t2m} of D13R02C₀₄₈ and D13R03C₀₄₈ with $\delta = +1$ mm are 0.59 and 0.52, respectively. These values are lower than the other results. On contrast, the R_{t2m} of D16R02T₀₆₆ and D16R03T₀₀₀ with $\delta = +3$ mm are 1.40, that is the highest of all. However, the average values of R_{t2m} are 0.91-1.12. Therefore, from the discussion in this section, it is concluded that the model can reasonably estimate the test results.

5 CONCLUSIOTN

In this study, the mechanical behavior of the interfaces with post-installed dowel bars and roughened surfaces by a vibratory hammer has been investigated. Moreover, the previous model [2] was modified to estimate the interfaces subjected to the compressive normal and shear stresses. The results of this study are described below.

Table 2: Test-to-model shear force ratio R_{t2m} .

Specimen ID	δ on positive side			δ on negative side		
	+1.0	+2.0	+3.0	-1.0	-2.0	-3.0
D13R01C ₀₄₈	0.87	0.84	0.99	1.00	1.00	1.06
D13R02C ₀₄₈	0.59	1.00	1.29	0.88	0.99	1.03
D13R03C ₀₄₈	0.52	0.88	1.19	-	1.01	1.31
D16R01C ₀₄₈	0.86	0.82	0.90	0.91	1.02	1.14
D16R02C ₀₄₈	0.79	0.84	1.09	0.79	0.91	1.05
D16R03C ₀₄₈	0.96	1.00	1.07	0.88	0.94	1.06
D13R01T ₀₀₀	0.83	0.88	0.96	0.90	0.86	0.87
D13R01T ₀₃₃	1.15	1.00	1.13	0.87	0.92	1.04
D13R01T ₀₆₆	1.22	1.05	1.16	0.99	0.89	1.09
D13R02T ₀₀₀	0.76	0.91	1.00	0.69	0.80	0.85
D13R02T ₀₃₃	1.05	1.18	1.28	1.05	1.18	1.28
D13R02T ₀₆₆	1.10	1.15	1.18	0.56	0.89	0.66
D13R03T ₀₀₀	0.92	0.92	1.11	0.75	1.00	1.07
D13R03T ₀₃₃	1.17	1.15	1.34	1.02	1.22	1.32
D13R03T ₀₆₆	1.31	1.22	1.32	1.08	1.01	1.17
D16R01T ₀₀₀	0.88	0.79	0.86	0.83	0.82	0.87
D16R01T ₀₃₃	1.19	0.81	0.91	1.05	0.93	0.99
D16R01T ₀₆₆	0.83	0.74	0.82	0.92	0.95	1.03
D16R02T ₀₀₀	1.10	0.91	1.02	0.89	1.04	1.17
D16R02T ₀₃₃	1.04	0.87	1.02	0.96	0.76	0.82
D16R02T ₀₆₆	1.08	1.20	1.40	0.93	1.20	1.13
D16R03T ₀₀₀	1.08	1.20	1.40	0.93	1.20	1.13
D16R03T ₀₃₃	1.01	1.10	1.31	0.92	0.92	1.02
D16R03T ₀₆₆	0.87	0.84	0.93	0.56	0.80	0.86
D19R01T ₀₀₀	1.24	1.10	1.09	1.22	1.18	1.21
D19R01T ₀₃₃	1.15	1.05	1.10	0.96	0.95	1.05
D19R01T ₀₆₆	1.16	0.95	1.04	0.98	1.05	1.14
D19R02T ₀₀₀	1.14	1.06	1.15	1.03	1.16	1.16
D19R02T ₀₃₃	1.41	1.06	1.17	0.57	1.01	1.07
D19R02T ₀₆₆	1.05	0.92	0.92	0.93	0.93	0.92
D19R03T ₀₀₀	1.08	1.17	1.29	0.98	1.13	1.12
D19R03T ₀₃₃	1.39	1.27	1.39	1.10	1.14	1.29
D19R03T ₀₆₆	1.30	1.04	1.13	1.06	1.04	1.00
Average	1.03	1.00	1.12	0.91	1.00	1.06

- 1) In order to apply the previous model [2] to the compressive normal stress, the envelope curve and the softening coefficient β , which was shown in Eq. (4), were modified. Furthermore, the constant shear stress after softening τ_{con} , which was shown in Eq. (5), was modified.
- 2) Point Z has been improved for estimating the reloading behavior of the specimen under compressive normal stress.
- 3) As the diameter of dowel bar d_d was smaller, the opening width of interfaces was wider. [1-2] To consider this effect, the coefficient K_α was added to the previous model.
- 4) For D13R02C₀₄₈ and D13R03C₀₄₈ with $d_d = 13$ mm and $\sigma_0 = -0.48$ N/mm², the large slip behavior was observed on the negative loading. Therefore, the model could not accurately estimate these test results.
- 5) With the increase of δ , the effect of dowel bar was intensified; whereas, under the

compressive normal stress, it became insignificant.

- 6) When comparing the analytical results with the test results, although some discrepancies were confirmed, the modified model could reasonably estimate the test results for most of the specimens. The average values of the ratio between the model and test results were 0.91-1.12.

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